

Expressiveness of SHACL Features

ICDT 2021

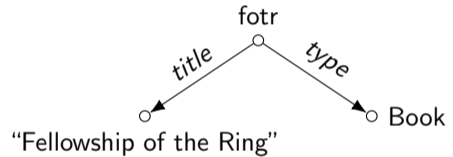
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Vrije Universiteit Brussel & Universiteit Hasselt

March 2022

SHACL

- **S**hapes **C**onstraint **L**anguage
- Constraint language for RDF graphs
- Conformance checking



SHACL

- **Shapes Constraint Language**
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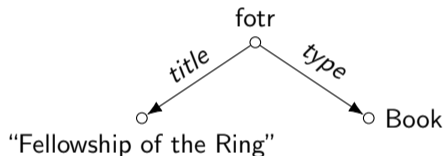
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:BookShape
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  a sh:PropertyShape;
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```
  sh:path :title;
```

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  sh:minCount 1.
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:BookShape sh:targetClass :Book
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$$\geq_1 \text{type.Book} \sqsubseteq \geq_1 \text{title.T}$$


SHACL

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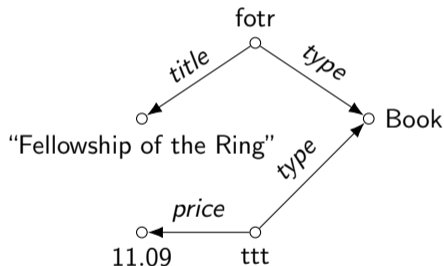
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SHACL shapes

The language \mathcal{L}

$$\phi ::= \top \mid \{c\} \mid \phi \wedge \phi \mid \phi \vee \phi \mid \neg \phi \mid \forall E.\phi \mid \geq_n E.\phi$$
$$E ::= p \mid p^- \mid E \cup E \mid E/E \mid E^*$$

E are regular path queries with inverse

SHACL shapes

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An interpretation I :

- domain Δ^I
- interprets *node names*
- interprets *property names*

ϕ	$I, a \models \phi$ if:
$\{c\}$	$a = \llbracket c \rrbracket^I$
$\geq_n E.\psi$	$\#\{b \in \llbracket E \rrbracket^I(a) \mid I, b \models \psi\} \geq n$
$\forall E.\psi$	every $b \in \llbracket E \rrbracket^I(a)$ must $I, b \models \psi$

SHACL shapes

The language $\mathcal{L}(eq, disj, closed, ?)$

$$\phi ::= \top \mid \{c\} \mid \phi \wedge \phi \mid \phi \vee \phi \mid \neg\phi \mid \forall E.\phi \mid \geq_n E.\phi \mid eq(p, E) \mid disj(p, E) \mid closed(Q)$$

$$E ::= p \mid p^- \mid E \cup E \mid E/E \mid E^* \mid E?$$

E are regular path queries with inverse

Distinctive features:

- Equality
- Disjointness
- Closure
- Zero-or-one path

ϕ	$I, a \models \phi$ if:
$\{c\}$	$a = \llbracket c \rrbracket'$
$\geq_n E.\psi$	$\#\{b \in \llbracket E \rrbracket'(a) \mid I, b \models \psi\} \geq n$
$eq(E, p)$	the sets $\llbracket E \rrbracket'(a)$ and $\llbracket p \rrbracket'(a)$ are equal
$disj(E, p)$	the sets $\llbracket E \rrbracket'(a)$ and $\llbracket p \rrbracket'(a)$ are disjoint
$closed(R)$	$\llbracket p \rrbracket'(a)$ is empty for each $p \in \Sigma - R$

SHACL shapes

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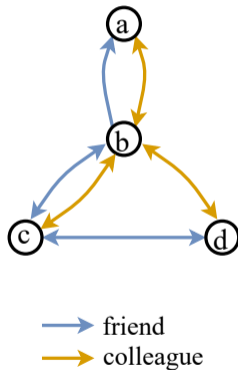
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Do we need these features in the language?

Example shapes

“Through a path of **friend** edges, the node can reach node *d*”

$$\phi \equiv \geq_1 \text{friend}^* . \{d\}$$

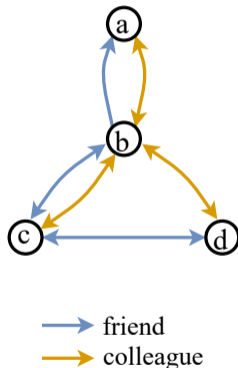


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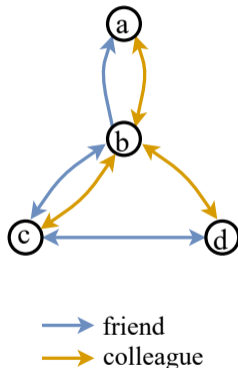
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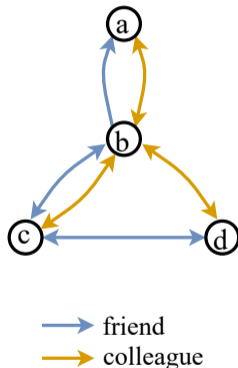
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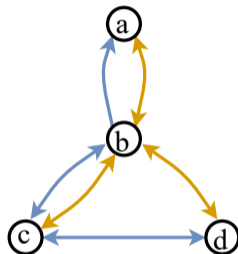
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“Nodes who have at least one **colleague** who is also a **friend** ”

$$\phi \equiv \neg \text{disj}(\text{friend}, \text{colleague})$$



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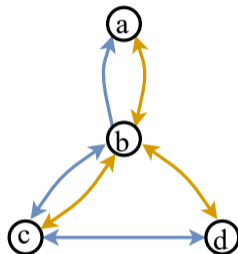
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$$\llbracket \phi \rrbracket^G = \{b, c\}$$



Graphs and interpretations

- A graph is a finite set of *facts*
- A fact is of the form $p(a, b)$ with p a property name and a, b nodes from the graph

We associate to any given graph an interpretation I :

- The domain is the universe of *all nodes*
- Every constant is interpreted as itself
- The interpretation of a property name is fixed by the facts

Shape schemas

A *shape schema* is a set of inclusion statements

$$\phi_t \subseteq \phi_s$$

A shape schema *defines* a class of graphs.

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Example: the class of symmetric graphs.

$$\geq_1 r.T \subseteq eq(r, r^-)$$

Main result: primitivity of the features

For each feature $X \in \{eq, disj, closed, ?\}$ we define a class of graphs Q_X such that:

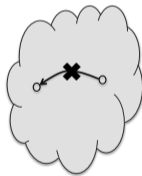
- Q_X is definable by a simple inclusion using only the feature X
- Q_X is **not** definable without X

Proving primitivity of equality

Equality

Q_{eq} is the class of symmetric graphs: $\geq_1 r.T \subseteq eq(r, r^-)$

Graph G



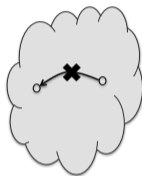
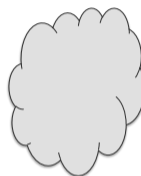
A complete directed graph
with one edge removed

Graph G'



A complete directed graph

Proving primitivity of equality

Graph G Graph G' 

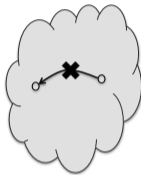
Lemma

Let H be G or G' . For every path expression E , we have:

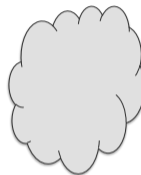
- $\llbracket E \rrbracket^H \supseteq \llbracket r \rrbracket^H$
- $\llbracket E \rrbracket^H \supseteq \llbracket r^- \rrbracket^H$
- $\llbracket E \rrbracket^H \supseteq V \times V$

Proving primitivity of equality

Graph G



Graph G'



Proposition

For any shape ϕ not using eq : $\llbracket \phi \rrbracket^G = \llbracket \phi \rrbracket^{G'}$.

Proving primitivity of disjointness

Disjointness

Q_{disj} is the class of graphs where all nodes have at least one symmetric edge:



$$\geq_1 r.T \subseteq \neg disj(r, r^-)$$

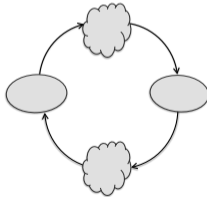
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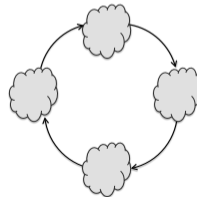
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Graph G



An alternating cycle of cliques

Graph G'

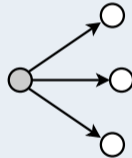


A cycle of cliques

Proving primitivity of zero-or-one paths

Zero-or-one paths

$Q_?$ is the class of graphs where all nodes have at least three outgoing edges not to themselves:



$$\geq_1 r.T \subseteq \geq_4 r?.T$$

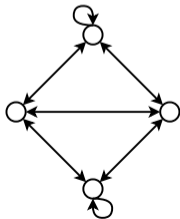
Proving primitivity of zero-or-one paths

Zero-or-one paths

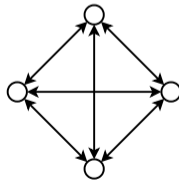
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Graph G



Graph G'



Proving primitivity of closure

Closure

Q_{closed} is the class of graphs where the only edge label allowed is r .

Proposition

Shapes without using closed do not distinguish between graphs that are equal on all edge labels mentioned in the shape.

Conclusion & Future Work

We established the primitivity of equality, disjointness, zero-or-one paths and closure in SHACL.

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Real SHACL has some hidden features:

- $eq(id, p)$ which is expressible as $eq(p?, p) \wedge \geq_1 p.\top \wedge \leq_1 p.\top$
- $disj(id, p)$ which is expressible as $\neg eq(p?, p)$
- Is zero-or-one path still primitive?

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We established the primitivity of equality, disjointness, zero-or-one paths and closure in SHACL.

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Natural extensions of the shape language:

- allow shapes of the form $eq(E_1, E_2)$ and $disj(E_1, E_2)$
- allow path expressions with *tests* (as in PDL)
- expressiveness under recursive semantics (stable model, well-founded)